# **THE LIGHT AND DARK SIDE OF GALAXY FORMATION**

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**ROSSI LECTURES 2014**

# INTRODUCTION BASIC ELEMENTS OF GALAXY FORMATION LIES, DAMNED LIES, AND SIMULATIONS

# **PHYSICS OF THE EARLY UNIVERSE**

The Cosmic Microwave Background as seen by Planck and WMAP





 $A_{\rm GW}\propto H\propto E_{\rm inf}^2\sim (10^{16}\,\text{GeV})^2$ 

JUST SIX NUMBERS (ΛCDM)  $\Omega_{\Lambda} = 0.681$  $\Omega_{\rm CDM}=0.27$  $\Omega_b = 0.049$  $H_0 = 67 \,\mathrm{km/s/Mpc}$  $\sigma_8 = 0.835$  $n_s = 0.96$  $\tau_e = 0.09$ 

INFLATION: THE "BANG" OF THE "BIG BANG"

tensor (gravitational waves)  $= 0.2 \pm 0.05$ scalar (density perturbations)





greater than onedegree scale



# **DARK MATTERS**



Most of the universe can't even be bothered to interact with you.

S. Carroll

From both astrophysical and particle physics considerations, stable and heavy *Weakly Interacting Massive Particles (WIMPs)* that arise from extensions to the SM of particle physics are particularly compelling.



# **A WIND OF WIMPS**



 $E_{\rm kin} = 0.5 \times (100 \,\text{GeV}) \times (220 \,\text{km/s})^2 = 27 \,\text{keV}$ 



# **SEEING THE INVISIBLE**



Galactic Center produces *more 1–3* GeV *gamma-rays* than can be explained by known sources.

Excess emission is consistent with a *30–40* GeV *WIMP* annihilating into *quarks* with a thermally-averaged cross-section *‹v›=(1.4–2.0) x 10-26* cm3/s!

> The Characterization of the Gamma-Ray Signal from the Central Milky Way: A Compelling Case for Annihilating Dark Matter

> > Tansu Daylan,<sup>1</sup> Douglas P. Finkbeiner,<sup>1,2</sup> Dan Hooper,<sup>3,4</sup> Tim Linden,<sup>5</sup> Stephen K. N. Portillo,<sup>2</sup> Nicholas L. Rodd,<sup>6</sup> and Tracy R. Slatyer<sup>6,7</sup>



# **PHYSICS OF GALAXY FORMATION**



# **FIRST GALAXIES**



# **COSMIC DROPOUTS**



### **COSMIC HISTORY OF STAR FORMATION**



Madau & Dickinson 2014

# **MBH ACCRETION HISTORY**



### **UNIVERSE IN A BOX: COSMOLOGICAL SIMULATIONS**

Time since Big Bang: 0.19 billion years



# **CF. WHEN I WAS AN UNDERGRAD IN ARCETRI…**



NO KNOWN *NORMAL* GALAXIES AT HIGH-REDSHIFT.

#### **RAPID PACE OF DISCOVERY** Keck First Data & **HST** upgrade 0.12 **HST HDF UDF** Launch 0.10 Fraction of publications 0.08 0.06  $0.04$  $0.02$ matching "galaxy evolution" Articles in Al & Apl matching cosmological parameter  $0.00$ 986 1982 1990 978 199 Year

Question: do more publications in a given field mean most key questions are being answered? Should new students move into less well-developed fields?

INTRODUCTION BASIC ELEMENTS OF GALAXY FORMATION LIES, DAMNED LIES, AND SIMULATIONS

# **FROM QUANTUM FOAM TO GALAXIES**



# **A RECIPE FOR GALAXY FORMATION**



### **STANDARD COSMOLOGICAL MODEL**

HOMOGENOUS, ISOTROPIC, EXPANDING UNIVERSE

$$
ds^2=-c^2dt^2+a^2(t)\left[\frac{dr^2}{1-kr^2}+r^2d\Omega^2\right]
$$

HUBBLE'S LAW *k=0* ➩ *Universe is flat a source located at separation R*

 $R = a(t)r$  $v=\dot{R}=\dot{a}r=\left(\frac{\dot{a}}{a}\right)R=HR.$  $\frac{\Delta \nu}{\nu} = -\frac{v}{c} = -\frac{\dot{a}}{a} \frac{R}{c} = -\frac{\dot{a}}{a} \Delta t$  $\nu \propto a^{-1}$ 

$$
\lambda = (c/\nu) \propto a = \frac{1}{(1+z)}
$$



# **FRIEDMANN EQUATIONS IN A FLAT UNIVERSE**

 $H^2 = \frac{8\pi G}{3} \rho = H_0^2 \left(\Omega_\mathrm{M} a^{-3} + \Omega_\Lambda + \Omega_\mathrm{R} a^{-4}\right)$  $\frac{\ddot{a}}{a}=-\frac{4\pi G}{3}(\rho+3p/c^2)=-\frac{H_0^2}{2}\left(\Omega_{\rm M} a^{-3}-\Omega_\Lambda+2\Omega_{\rm R} a^{-4}\right)$ 



The cosmological parameters describing the Universe at recombination can be summarized on a single sheet of paper. Yet the most detailed supercomputer simulation cannot fully describe the complex structures we see today.....Why?

# **GRAVITATIONAL INSTABILITY IN A NUTSHELL**

Let ρ*(x)* be the density distribution of matter at location *x*

Let  $\delta(x)$  be the corresponding overdensity field  $\delta(\vec{x}) = \frac{\rho(\vec{x})}{\bar{\rho}} - 1$ 

NB: δ*(x)* is the outcome of some random process in the early Universe like *quantum fluctuations of the inflaton field!*



non-linear regime |δ*|*≿*1*

According to linear theory, the density field evolves as density field linearly

$$
\delta(\vec{x},t) = D(t)\delta_0(\vec{x}) \ll
$$



According to the spherical collapse model in a  $\Omega_M = I$  Universe, regions with  $\delta(x,t) > \delta_c = 1.696$  will have collapsed to produce dark matter halos by time *t*. QUESTION: which halos will collapse first?

|The perturbed density field can be written  $\,\,\lambda=2\pi a/k\,$ as a sum of plane waves of different *wave numbers* (called *modes*) which evolve  $\delta(\vec{x}) = \sum \delta_{\vec{k}} e^{i\vec{k}\cdot\vec{x}}$ independently in the linear regime

The variance of the density field can then be written as

Note: *P(k)* has units of volume!

$$
\sigma^2 = \langle \delta^2 \rangle = \frac{1}{(2\pi)^3} \int P(k) d^3 \vec{k} = \frac{1}{2\pi^2} \int P(k) k^2 dk
$$

*P(k) is the power spectrum* . Inflation predicts an initial power spectrum of the form

$$
P(k) \propto k^n \quad n \lesssim 1 \quad \text{Scale INVARIANT} \over \text{Planck} \rightarrow n = 0.96
$$

The index *n* governs the balance between large- and small-scale power in the Universe.



The meaning of different values of *n* can be seen by imagining the results of *smoothing* the density field by passing over it a box of some characteristic *comoving size R* and averaging the density field over the box.

This will filter out waves with *k*≿*1/R*, leaving a variance

$$
\langle \delta_R^2 \rangle \propto \int_0^{1/R} \widehat{ \langle k^n k^2 dk } \propto R^{-(n+3)}.
$$

Hence, in terms of a mass , we have

$$
M \propto R^3
$$



$$
\langle \delta_M^2 \rangle^{1/2} \propto M^{-(n+3)/6}
$$

NB: we do not observe the primordial *P(k)* but *P(k)T(k)*. In CDM, *P(k)* is suppressed on small scales during the radiation-dominated era,  $P(k) \sim k^{n-4}$ .... Density Fluctuation Data Agree with ACDM



Mass scale M [Msolar]

# **LINEAR GROWTH OF DM PERTURBATIONS**



static  $H=0$  Universe  $\Leftrightarrow$  mode grows exponentially with time

 $\delta_+ \propto e^{t/t_c}$ 

flat, matter-dominated Universe *H=2/3t*

$$
\delta_+\propto a=1/(1+z)
$$

 $\Rightarrow$  growth is algebraic instead of exponential!

flat, Λ-dominated Universe *H=const*

$$
\ddot{\delta}_k + 2H\dot{\delta}_k = 0 \rightarrow \delta_+ = \mathrm{const}
$$

perturbations are now frozen!

### **GALAXY FORMATION: A 2-STEP PROCESS**



### **SPHERICAL COLLAPSE IN A Ω***M=1* **UNIVERSE**



Think of an overdensity as consisting of many individual, thin mass shells  $\Rightarrow$  ONION MODEL





Because of collisionless nature of the DM, the shell crosses itself and starts to oscillate ➩ VIOLENT RELAXATION/ VIRIALIZATION

 $2K+W=0$ 

## **STRUCTURE FORMATION: AN N-BODY SIMULATION OF LARGE-SCALE STRUCTURE IN A ΛCDM COSMOLOGY**

### note the formation of pancakes, filaments and halos, and how voids become more spherical with time….

# **TIMESCALES OF GALAXY FORMATION**

HUBBLETIME	$t_H = H^{-1} = H_0^{-1} [\Omega_M (1+z)^3 + \Omega_{\Lambda}]^{-1/2}$	
FREE-FALL TIME	$t_H = \sqrt{3\pi/32G\rho}$	\n $\rho = \rho_b + \rho_{DM} \equiv \Delta \rho_{crit}$ \n
EXEC-FALL TIME	$t_{\text{ff}} = \sqrt{3\pi/32G\rho}$	\n $t_{\text{ff}} = 1.57 t_H/\sqrt{\Delta}$ \n
QOOLING TIME	$t_{\text{cool}} = \frac{3nk_B T}{2n_H^2 \Lambda(T)} \propto n^{-1}$	\n $\Rightarrow$ denser gas cools faster
3 REGIMES	3 REGIMES	cooling is not important, gas in hydrostatic equilibrium
b) $t_{\text{ff}} < t_{\text{cool}} < t_{\text{H}}$	\n $\frac{\text{system evolves on cooling timescale. Gas contracts}}{\text{slowly as it cools.}}$ \n	

cooling is catastrophic, gas cannot respond to loss of pressure and falls to the center on the free-fall timescale. c)



# **COLD MODE ACCRETION**


## M<sub>VIR</sub><10<sup>12</sup> M<sub>®</sub> LIKE IT COLD!







#### **BARYONS MATTER: FEEDBACK**



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#### **COSMIC RELICS**



#### *N***-BODY COSMOLOGICAL SIMULATIONS OF A GALAXY HALO**

- assume all Ω*M* is in cold WIMPs, and sample it with *N* particles.
- bad approximation in the center of a massive galaxy where baryons dominate, OK for ultra-faint dwarfs (*M/L~1000*).
- simple physics (just gravity) & good CPU scaling  $\Rightarrow$  high spatial and temporal resolution.
- no free parameters (ICs known from CMB and LSS)

#### ➪ ACCURATE SOLUTION TO AN IDEALIZED PROBLEM





#### **HIERARCHICAL N-BODY TREE CODES**

# OCTREE gravity calculation<br> $O(N^2) \Rightarrow O(N \log N)$

Newton's equations of motion in co-moving coordinates

$$
\frac{\mathrm{d}\vec{x}}{\mathrm{d}t} = \vec{v}
$$

$$
\frac{\mathrm{d}\vec{v}}{\mathrm{d}t} + 2H(a)\vec{v} = -\frac{1}{a^2}\vec{\nabla}\phi.
$$

Cosmology, the expansion of the universe

 $H(a) = \dot{a}/a$  (Hubble constant)  $\frac{\ddot{a}}{a}=-\frac{4}{3}\pi G\rho_{b}(t)+\frac{\Lambda}{3}\ \ {\rm (2^{nd}\,\, Friedman\,\, equation)}$ 

Gravitational potential

$$
\nabla^2 \phi = 4\pi G \rho a^2 - \Lambda a^2 + 3a\ddot{a}
$$

$$
= 4\pi G (\rho - \rho_b) a^2
$$



#### **ZOOMING-IN**



#### **STRUCTURE FORMATION: AN** *N***-BODY SIMULATION OF THE ASSEMBLY OF A MILKY WAY HALO**

# note the accretion of matter along filaments and the clumpiness of the final DM distribution…..

Stadel, Potter et. al. 2008

#### **RESOLUTION, RESOLUTION, RESOLUTION**



#### **RESOLUTION, RESOLUTION, RESOLUTION**

#### **RESOLUTION, RESOLUTION, RESOLUTION**



#### **INCOMPLETELY PHASE-MIXED MATERIAL**



DEBRIS FLOWS (SHELLS, SHEETS, PLUMES)

#### **THE WIMP MIRACLE**





William I: 
$$
r_s = 180 \text{ pc}, \rho_s = 0.4 \text{ M}_{\odot} \text{ pc}^{-3}
$$
  
\n $m_{\chi} = 150 \text{ GeV}$   $d = 38 \text{ kpc}$   
\n $L_{\text{ann}}^{\text{WI}} = \frac{\langle \sigma v \rangle}{m_{\chi}} \left(\frac{4\pi}{3}\right) r_s^3 \rho_s^2 \sim 10^{35} \text{ ergs s}^{-1}$ 

#### **WIMP ANNIHILATION SIGNAL**





#### **THE SMALL-SCALE CRISIS**



#### Invisible galaxy said likely made of dark matter

#### MISSING SATELLITE PROBLEM



Mass (solar masses)







#### WHY DO WE CARE ABOUT DWARFS?

• DGs are cosmic DM laboratories: probe the power spectrum on small scales and offer a unique test of the particle nature of the dark matter.

• DGs are the champions of the epoch of first light: first generation of cosmic structures to go nonlinear  $\Rightarrow$ believed to be responsible for the reionization and chemical enrichment of the early universe.



#### ERIS SIMULATION OF A MW GALAXY

#### $M_{\rm vir}=8\times10^{11}\,{\rm M}_\odot$  $N = 13M (DM) + 13M (SPH)$

Pillepich et al 2014

#### Guedes et al 2011

• DGs are the building blocks of massive galaxies: their remnants provide a powerful test of the hierarchical assembly of cosmic structures.



$$
z_i = 0.77, M_{\text{vir}} = 9 \times 10^9 \text{ M}_{\odot}
$$
\n
$$
M_* = 2.6 \times 10^8 \text{ M}_{\odot}
$$
\n
$$
z = 0, M_{\text{vir}} = 3.4 \times 10^7 \text{ M}_{\odot}
$$
\n
$$
M_* = 2.2 \times 10^7 \text{ M}_{\odot}
$$
\n
$$
= 0.77, M_{\text{vir}} = 3.4 \times 10^7 \text{ M}_{\odot}
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#### TRACTIVE SOLUTION TO THE **G PROBLEM: BARYONS**

**●** Until recently any direct effect of the baryonic component on the DM was limited to a minor *adiabatic* correction, i.e. baryonic processes modulate the SFR without changing the underlying DM scaffolding.

*●* This picture has recently been subverted. Spectroscopic observations have revealed the ubiquity of *galaxyscale outflows*, even in dwarfs with *SFR«1M*⦿*/yr*. It has been realized that these processes have a *non-adiabatic* impact on the host DM halo.



#### CAN SUPERNOVA FEEDBACK FIX DM DENSITIES? EXPLAIN LOW SFES?

- *●* Capturing the baryonic and feedback processes that regulate the *metabolism* of DGs requires cosmological hydro simulations of high dynamic range.
- *●* Gas in such *low-Z* systems does not settle into a *thin, cold disk,* and their shallow potential wells make the ISM more prone to disruption from energetic SNe.
- *●* Star formation may proceed in a *bursty* manner that is different from that of larger mass spirals.
- *●* Stellar feedback drives *galactic outflows* that modulate the stellar buildup, lower *fgas* and alter the chemical evolution of  $DGs$ .





#### FEEDBACK

*●* Each SN deposits metals and  $E\simeq 10^{51}$  ergs (Kroupa IMF  $\left|\right|$  SN/87 <sub>10</sub>  $M_{\odot}$ ) into the nearest neighbors (1-2  $R_S$  [pc] SPH particles). (log scale)

*●* SN feedback: heated gas has its cooling shut off  $\Rightarrow$  galactic ouflows

*t*blast*=106.85 E510.32 n-0.16P04-0.2* yr *R*blast=*101.74 E510.32 n0.34P04-0.7* pc  $(t_{\rm cool} \sim T^{1/2}$  above 1 keV)

*minimalistic feedback*: cf. explicit wind particles/mass+metal loading/ 2-phase subgrid ISM/radiation pressure on dust/AGN feedback/ hydro decoupling (e.g. Vogelsberger et al. 2013).



### A GROUP OF SEVEN DWARFS

- *●* LCDM cosmological SPH simulation run to *z=0*
- $\bullet$  mass  $m_{\rm DM} = 1.6 \times 10^4 \,\rm M_{\odot}$  $\mathsf{l}$ resolution  $\,m_* = 1000 \, {\rm M}_{\odot}$



- *●* gravitational softening=86 ppc
- *●* metal-dependent gas cooling
- *●* UVB heating & photoionization

*●* high SF gas density threshold of 100 cm<sup>-3</sup>  $\Rightarrow$  SF is clustered<br> $d\rho_*/dt = 0.1 \times (\rho_{\rm gas}/t_{\rm dyn}) \propto \rho_{\rm gas}^{3/2}$ 

$$
\lambda_{\rm J,th} = (\pi c_s^2/G\rho)^{1/2} \approx 50 T_3^{1/2}\, {\rm pc}
$$



# **GRID**



# $\rho(\mathbf{r}) = \sum_{j=1}^{N} m_j W(|\mathbf{r}-\mathbf{r}_j|, h)$  KEY FEATURES OF SPH

• An exact solution to the continuity equation.

● RESOLUTION follows mass, particle nature gives natural compatibility with N-body codes.

● ZERO intrinsic dissipation/numerical diffusion. Need to add some explicitly to: 1) capture shocks; 2) avoid suppression of fluid mixing.

● EXACT conservation of mass, momentum, angular momentum, entropy.

● ADVECTION done perfectly. Galilean invariance -- important in cosmological simulations where highly supersonic bulk flows are common.

● Does not CRASH ("screw-ups" indicated by noise rather than code crash).

● Gas particles have "NAMES".

#### TURBULENT DIFFUSION OF METALS AND THERMAL ENERGY



$$
(dc/dt)_D = (1/\rho)\nabla \cdot (D\nabla c)
$$
  

$$
D = 0.05 \,\rho |S_{ij}| h^2
$$

*Sij=*trace-free velocity shear tensor  $\Rightarrow$  no diffusion for compressive or purely rotating flow (Shen et al 2010)



WORD OF CAUTION: MW HALO GAS DOES NOT **MIX WELL!** 



Tobias Westmeler, CSIRO Australia Telescope National Facility Based on the Leiden/Argentine/Bonn Survey (Kalberla et al. 2005, A&A 440, 775) and the Milky Way model of P. Kalberla (Kalberla et al. 2007, A&A, in press).









#### THE STELLAR MASS FRACTION OF DGS AT Z=0.









GASOLINE VS. ENZO

 $\dot{\rho}_{*} \propto \rho_{\rm gas}^{3/2}$  vs.  $\dot{\rho}_{*} \propto f_{\rm H2} \rho_{\rm gas}^{3/2}$ 





Average ANGST dIrr formed bulk of its stars prior to *z=1,* exhibits ancient star formation (>10 Gyr ago) and lower levels of activity over the last 6 Gyr.



Low star formation efficiencies *are not the result of blowing away* all the baryons. Baryons are retained *but are unable to make stars* because of the more realistic description of where stars form (in high density clouds) and how feedback regulates the thermodynamics of the ISM.



#### METAL POOR

Stellar metallicity *V-*band luminosity relation for Milky Way's dSphs (Kirby et al. 2011).

The stellar mass-gas phase metallicity relation of DGs. Fraction of all the metals ever produced retained increases with decreasing stellar mass  $= 10\%$ —90% for Bashful-Dopey.

![](_page_71_Figure_0.jpeg)

#### **CORED PROFILE**

$$
\rho_{\rm DM}=\frac{\rho_0}{1+(R/R_c)^2}
$$

 $R_c = 1.8 \,\text{kpc}$  $= 2.1 \,\mathrm{kpc}$




## BURSTY STAR FORMATION & POTENTIAL FLUCTUATIONS



The bursty star formation histories of DGs. Bottom left panel: fluctuating baryonic (gas+stars) central masses of the two simulated DGs.



## **THE END**